Overall Story

- Accelerating charges generate free space electromagnetic waves.
- Light is an EM wave and can be reflected and refracted.
- Mirrors and lenses form images of objects by collecting rays emitted from an object through reflection or refraction.

Maxwell's Equations

$$\oint \vec{\mathbf{E}}.d\vec{\mathbf{A}} = \frac{Q}{\varepsilon_0}$$

Gauss' Law

$$\oint \vec{\mathbf{B}}.d\vec{\mathbf{A}} = 0$$

Gauss' Law for Magnetism – no magnetic monopoles

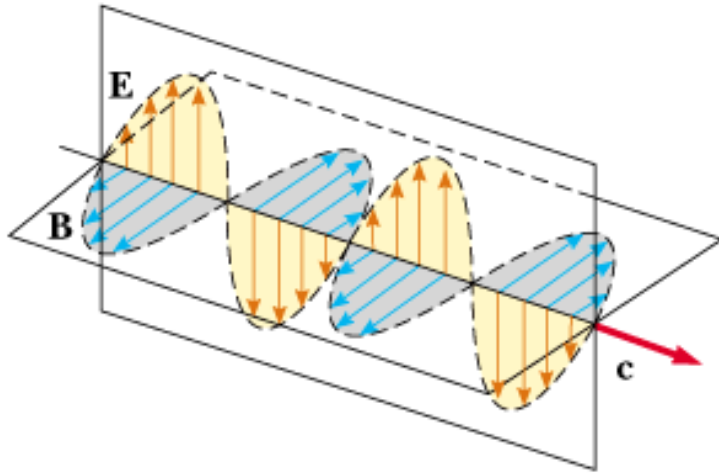$$\oint \vec{\mathbf{E}}.d\vec{\mathbf{s}} = -\frac{d\Phi_B}{dt}$$

Faraday's Law

$$\oint \vec{\mathbf{B}}.d\vec{\mathbf{s}} = \mu_0 I + \mu_0 \varepsilon_0 \frac{d\Phi_E}{dt}$$

Ampère-Maxwell Law

$$\vec{\mathbf{F}} = q\vec{\mathbf{E}} + q\vec{\mathbf{v}} \times \vec{\mathbf{B}}$$

Lorentz Force Law

EM Waves

$$E = E_{max} \cos(kx - \omega t)$$

$$B = B_{max} \cos(kx - \omega t)$$

$$\frac{E}{B} = \frac{E_{max}}{B_{max}} = \frac{\omega}{k} = c$$

$$c = \frac{1}{\sqrt{\mu_0 \varepsilon_0}}$$ Speed of Light

$$\omega = 2\pi f$$ Angular Frequency

$$\lambda = \frac{c}{f}$$ Wavelength

$$k = \frac{2\pi}{\lambda}$$ Wavenumber

$$\frac{\omega}{k} = c$$

Energy Carried by EM Waves

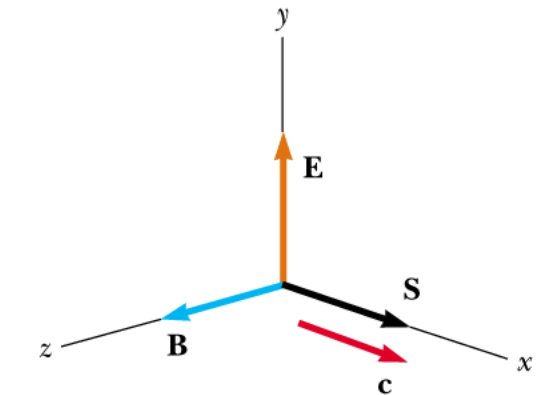$$\vec{S} = \frac{1}{\mu_0}\vec{E}\times\vec{B}$$ Poynting Vector (W/m²)

$$S = \frac{EB}{\mu_0} = \frac{E^2}{\mu_0 c} = \frac{c}{\mu_0}B^2$$

$$I = S_{av} = \frac{E_{max}B_{max}}{2\mu_0} = \frac{E_{max}^2}{2\mu_0 c} = \frac{c}{2\mu_0}B_{max}^2$$

$$u_E = u_B = \frac{1}{2}\varepsilon_0 E^2 = \frac{B^2}{2\mu_0}$$

$$u = u_E + u_B = \varepsilon_0 E^2 = \frac{B^2}{\mu_0}$$

$$u_{av} = \varepsilon_0\left(E^2\right)_{av} = \frac{1}{2}\varepsilon_0 E_{max}^2 = \frac{B_{max}^2}{2\mu_0}$$

$$I = S_{av} = cu_{av}$$

Momentum and Radiation Pressure

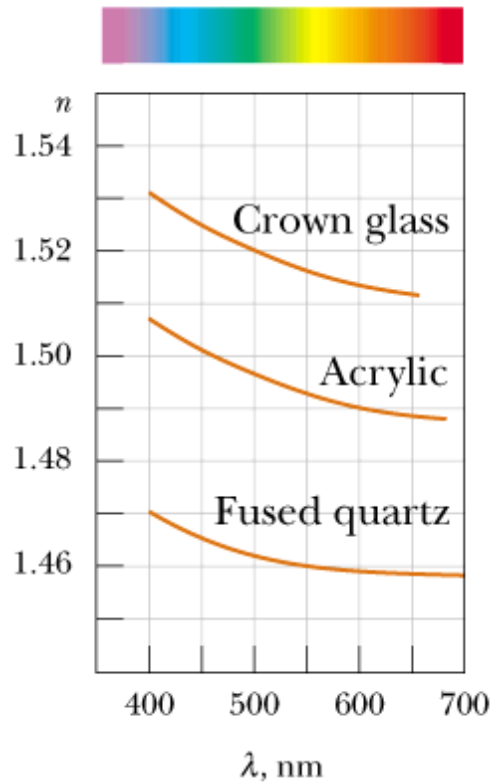|	Momentum	Pressure
Complete Absorption	$p = \dfrac{U}{c}$	$P = \dfrac{F}{A} = \dfrac{1}{A}\dfrac{dp}{dt} = \dfrac{S}{c}$
Complete Reflection	$p = \dfrac{2U}{c}$	$P = \dfrac{2S}{c}$

Reflection and Refraction

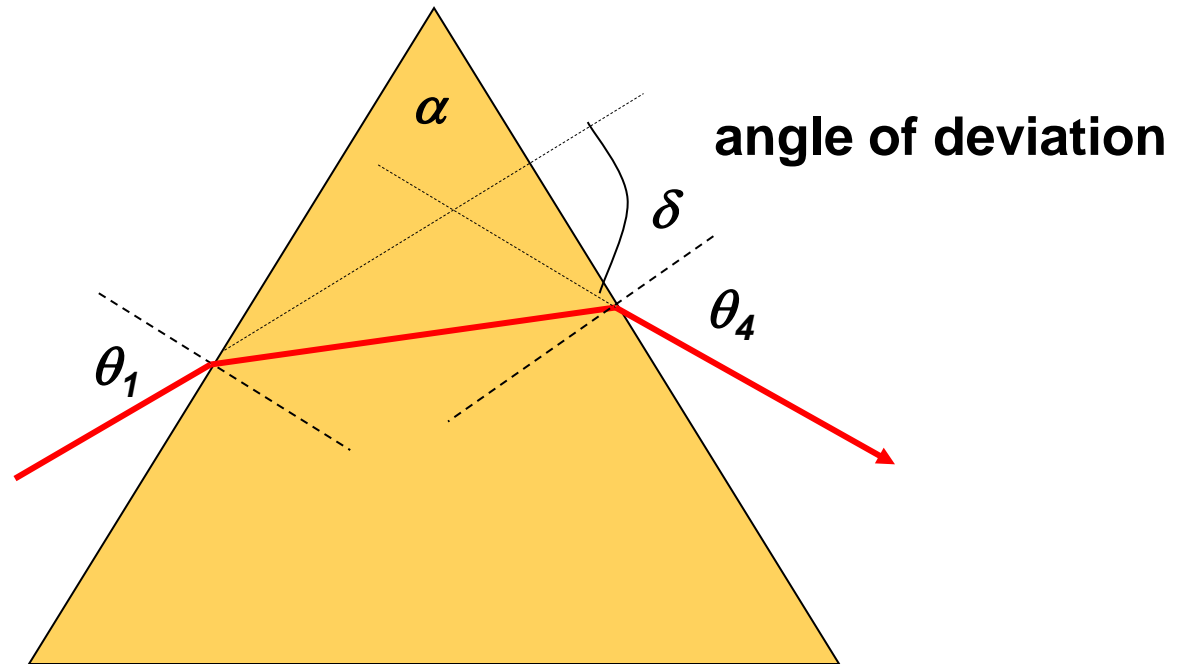$$\theta_1' = \theta_1$$

$$n = \frac{c}{v}$$

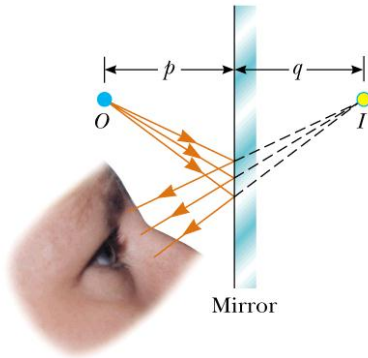$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\sin \theta_c = \frac{n_2}{n_1}$$

Dispersion and Prisms

$$n = n(\lambda)$$

Images by Mirrors

$$p = q$$

$$M = 1$$
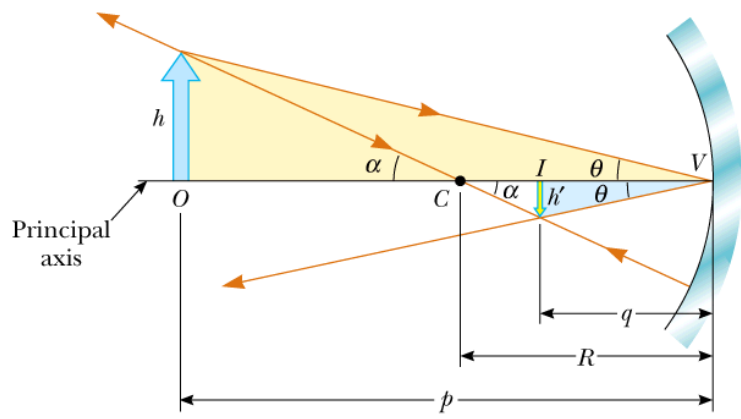
Front, or real, side | Back, or virtual, side

p and q positive | p and q negative
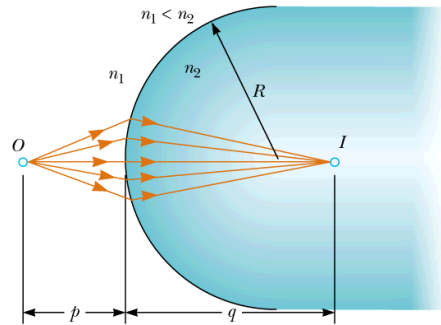
Incident light →

← Reflected light | No light

Convex or concave mirror

h

α | I | θ | V

α | h' | θ

Principal axis

O | C

q

R

p

Front | Back

O | I | F | C

p | q

$$\frac{1}{p} + \frac{1}{q} = \frac{1}{f}$$

$$f = \frac{R}{2}$$

$$M = \frac{h'}{h} = -\frac{q}{p}$$

Mirror

O | I

p | q

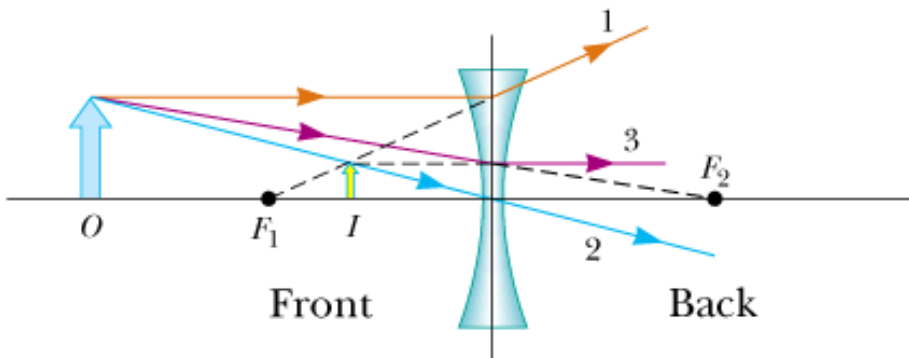# Images by Refraction and Lenses

$$\frac{n_1}{p} + \frac{n_2}{q} = \frac{(n_2 - n_1)}{R}$$

$$\frac{1}{p} + \frac{1}{q} = \frac{1}{f}$$

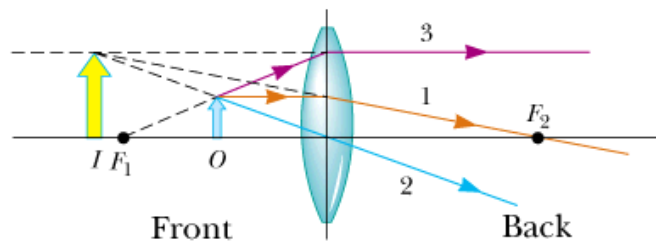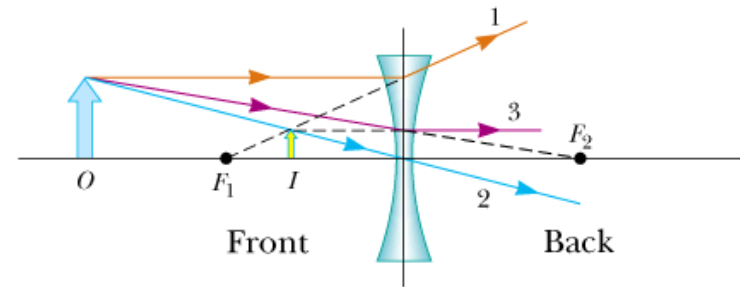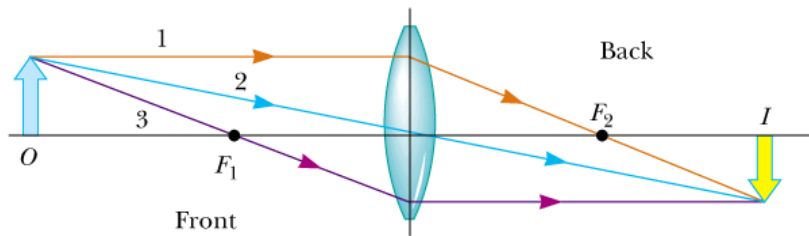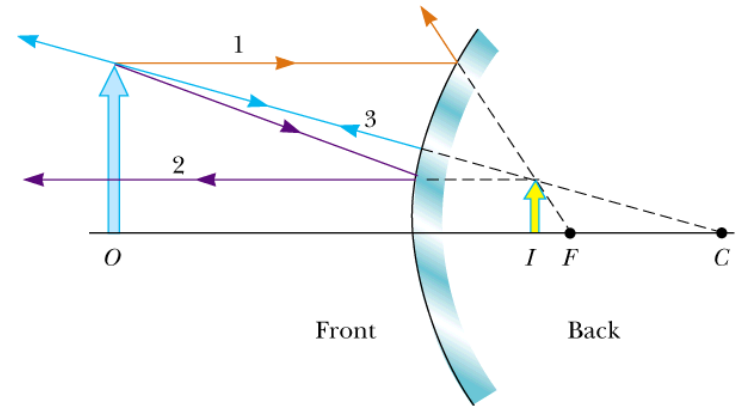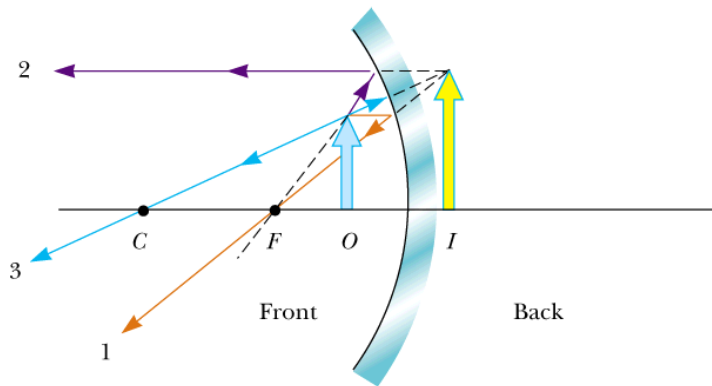$$\frac{1}{f} = (n-1)\left(\frac{1}{R_1} - \frac{1}{R_2}\right)$$
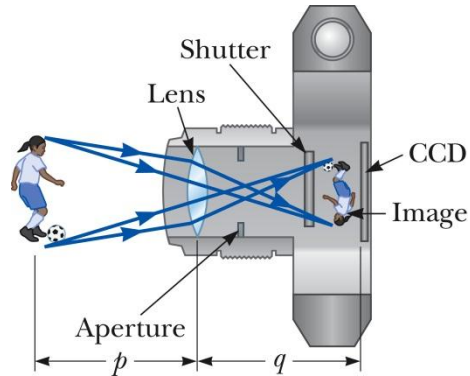
$$M = \frac{h'}{h} = -\frac{q}{p}$$

Ray Diagrams

Optical Instruments

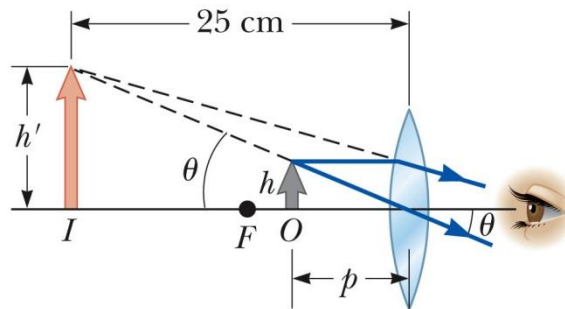The Camera

$$I \propto D^2 \big/ f^2$$
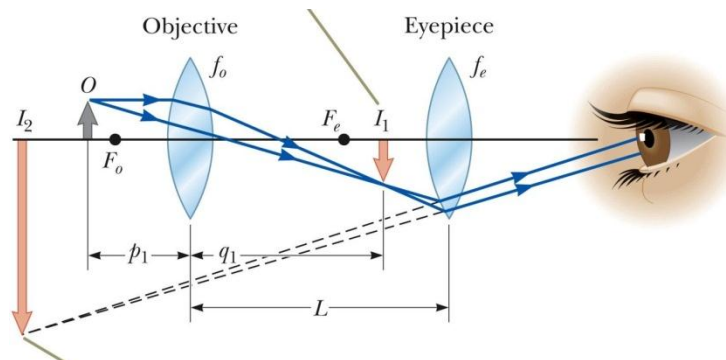
$$f - number = \frac{f}{\#} = \frac{f}{D}$$

Magnifier

$$m_\theta \approx \frac{25cm}{f}$$

Compound Microscope

$$M = -\frac{p_1}{f_o} \frac{25cm}{f_e}$$